

**Atmospheric Sciences 3510**

**Midterm Exam**

April 13, 2010

100 points

You may use your skew- $T$  log  $p$  diagram for any problem for which it is applicable. You may be specifically asked to use it for some problems. A list of physical constants follows the problems.

1. (40 points) A parcel ascends adiabatically over a mountain range starting from 1000 mb, where  $T = 29.5^\circ \text{ C}$  and mixing ratio =  $14 \text{ g kg}^{-1}$ , to 550 mb. Then it descends adiabatically back down to 1000 mb.

(a) Complete the following table of parcel properties. The parcel ascends from time 1 to time 4, then descends. from time 4 to time 6.

time (arbitrary units)	1	2	3	4	5	6
pressure (mb)	1000		650	550		1000
temperature ( $T$ , $^\circ \text{ C}$ )	29.5					
dewpoint temperature ( $T_d$ , $^\circ \text{ C}$ )						
saturation mixing ratio ( $w_s$ , g/kg)		14			10	
water vapor mixing ratio ( $w$ , g/kg)	14	14			10	10
liquid water mixing ratio ( $w_l$ , g/kg)	0					
total water mixing ratio ( $w + w_l$ , g/kg)	14		12	10	10	
Relative humidity (percent)		100	100	100	100	

(b) Plot the parcel's temperature and dewpoint temperature versus pressure during ascent and descent on the accompanying skew- $T$  log  $p$  diagram. *Label each point with its corresponding time.*

2. (10 points) (a) For  $p = 900 \text{ mb}$ ,  $T = 15^\circ \text{ C}$ , and  $T_d = 5^\circ \text{ C}$ , use the skew- $T$  log  $p$  diagram to determine mixing ratio ( $w$ ) and relative humidity.

(b) For  $p = 1000 \text{ mb}$ ,  $T = 21^\circ \text{ C}$ , and  $w = 5 \text{ g kg}^{-1}$ , use the skew- $T$  log  $p$  diagram to determine dewpoint temperature ( $T_d$ ) and relative humidity.

3. (8 points) Use the skew- $T$  log  $p$  diagram (or calculations) to determine the saturation vapor pressure ( $e_s$ ) for  $T = -5, 5, 15$ , and  $25^\circ \text{ C}$ .

$T$	$-5^\circ \text{ C}$	$5^\circ \text{ C}$	$15^\circ \text{ C}$	$25^\circ \text{ C}$
$e_s(T)$				

4. (20 points) (a) A parcel ascends adiabatically from 1000 mb, where  $T = 32^\circ \text{C}$  and mixing ratio =  $12 \text{ g kg}^{-1}$  to 500 mb. For this parcel, use the skew- $T \log p$  diagram to determine the:

saturation pressure* ( $p_s$ )	
saturation temperature* ( $T_s$ )	
temperature at $p = 500 \text{ mb}$	
potential temperature at $p = 500 \text{ mb}$	
water vapor mixing ratio at $p = 500 \text{ mb}$	
equivalent potential temperature ( $\theta_e$ )	
wet-bulb potential temperature ( $\theta_w$ )	

\* at LCL

- (b) For this parcel, *calculate* the equivalent potential temperature ( $\theta_e$ ). Please *show your calculations*.

- (c) Recall that the formula for calculating  $\theta_e$  is an approximation. How much does your calculated value differ from the (more accurate) value obtained from the skew- $T \log p$  diagram?

5. (12 points) Rain falls into subsaturated air and eventually isobarically saturates and cools the air due to evaporation. The initial air temperature is  $T = 40^\circ \text{C}$ , the initial dewpoint temperature is  $T_d = 13.8^\circ \text{C}$ , and the pressure is  $p = 1000 \text{ mb}$ .

- (a) What is the air temperature after it is saturated and cooled?

- (b) What is the water vapor mixing ratio after the air is saturated and cooled?

- (c) How much rain water per unit mass of air evaporates to saturate and cool the air?

6. (10 points) A sling psychrometer measures temperature  $T = 26^\circ \text{C}$  and wet-bulb temperature  $T_w = 18^\circ \text{C}$  at a pressure of 1000 mb. Use the the skew- $T \log p$  diagram to determine the dewpoint  $T_d$ , mixing ratio  $w$ , and relative humidity.

## Useful constants

$$0^\circ \text{ C} = 273 \text{ K}$$

$$g = 9.8 \text{ m s}^{-2} \text{ (acceleration of gravity)}$$

$$\rho_w = 1000 \text{ kg m}^{-3} \text{ (density of liquid water)}$$

$$c_w = 4186 \text{ J kg}^{-1} \text{ K}^{-1} \text{ (specific heat capacity of liquid water)}$$

$$c_p = 1004 \text{ J kg}^{-1} \text{ K}^{-1} \text{ (specific heat at constant pressure for dry air)}$$

$$c_v = 717 \text{ J kg}^{-1} \text{ K}^{-1} \text{ (specific heat at constant volume for dry air)}$$

$$R_d = c_p - c_v = 287 \text{ J kg}^{-1} \text{ K}^{-1} \text{ (gas constant for dry air)}$$

$$R^* = 8.31 \text{ J mol}^{-1} \text{ K}^{-1} \text{ (universal gas constant)}$$

$$m_d = 28.97 \text{ g mol}^{-1} \text{ (mean molecular weight of dry air)}$$

$$m_v = 18.02 \text{ g mol}^{-1} \text{ (molecular weight of water vapor)}$$

$$L_e = 2.5 \times 10^6 \text{ J kg}^{-1} \text{ (latent heat of evaporation)}$$