

Atmospheric Sciences 3510

Midterm Exam

April 13, 2010

100 points

You may use your skew- T log p diagram for any problem for which it is applicable. You may be specifically asked to use it for some problems. A list of physical constants follows the problems.

1. (40 points) A parcel ascends adiabatically over a mountain range starting from 1000 mb, where $T = 29.5^\circ \text{ C}$ and mixing ratio = 14 g kg^{-1} , to 550 mb. Then it descends adiabatically back down to 1000 mb.

(a) Complete the following table of parcel properties. The parcel ascends from time 1 to time 4, then descends. from time 4 to time 6.

time (arbitrary units)	1	2	3	4	5	6
pressure (mb)	1000		650	550		1000
temperature (T , $^\circ \text{ C}$)	29.5					
dewpoint temperature (T_d , $^\circ \text{ C}$)						
saturation mixing ratio (w_s , g/kg)		14			10	
water vapor mixing ratio (w , g/kg)	14	14			10	10
liquid water mixing ratio (w_l , g/kg)	0					
total water mixing ratio ($w + w_l$, g/kg)	14		12	10	10	
Relative humidity (percent)		100	100	100	100	

(b) Plot the parcel's temperature and dewpoint temperature versus pressure during ascent and descent on the accompanying skew- T log p diagram. *Label each point with its corresponding time.*

2. (10 points) (a) For $p = 900 \text{ mb}$, $T = 15^\circ \text{ C}$, and $T_d = 5^\circ \text{ C}$, use the skew- T log p diagram to determine mixing ratio (w) and relative humidity.

(b) For $p = 1000 \text{ mb}$, $T = 21^\circ \text{ C}$, and $w = 5 \text{ g kg}^{-1}$, use the skew- T log p diagram to determine dewpoint temperature (T_d) and relative humidity.

3. (8 points) Use the skew- T log p diagram (or calculations) to determine the saturation vapor pressure (e_s) for $T = -5, 5, 15$, and 25° C .

T	-5° C	5° C	15° C	25° C
$e_s(T)$				

4. (20 points) (a) A parcel ascends adiabatically from 1000 mb, where $T = 32^\circ \text{C}$ and mixing ratio = 12 g kg^{-1} to 500 mb. For this parcel, use the skew- $T \log p$ diagram to determine the:

saturation pressure* (p_s)	
saturation temperature* (T_s)	
temperature at $p = 500 \text{ mb}$	
potential temperature at $p = 500 \text{ mb}$	
water vapor mixing ratio at $p = 500 \text{ mb}$	
equivalent potential temperature (θ_e)	
wet-bulb potential temperature (θ_w)	

* at LCL

- (b) For this parcel, *calculate* the equivalent potential temperature (θ_e). Please *show your calculations*.

- (c) Recall that the formula for calculating θ_e is an approximation. How much does your calculated value differ from the (more accurate) value obtained from the skew- $T \log p$ diagram?

5. (12 points) Rain falls into subsaturated air and eventually isobarically saturates and cools the air due to evaporation. The initial air temperature is $T = 40^\circ \text{C}$, the initial dewpoint temperature is $T_d = 13.8^\circ \text{C}$, and the pressure is $p = 1000 \text{ mb}$.

- (a) What is the air temperature after it is saturated and cooled?

- (b) What is the water vapor mixing ratio after the air is saturated and cooled?

- (c) How much rain water per unit mass of air evaporates to saturate and cool the air?

6. (10 points) A sling psychrometer measures temperature $T = 26^\circ \text{C}$ and wet-bulb temperature $T_w = 18^\circ \text{C}$ at a pressure of 1000 mb. Use the the skew- $T \log p$ diagram to determine the dewpoint T_d , mixing ratio w , and relative humidity.

Useful constants

$$0^\circ \text{ C} = 273 \text{ K}$$

$$g = 9.8 \text{ m s}^{-2} \text{ (acceleration of gravity)}$$

$$\rho_w = 1000 \text{ kg m}^{-3} \text{ (density of liquid water)}$$

$$c_w = 4186 \text{ J kg}^{-1} \text{ K}^{-1} \text{ (specific heat capacity of liquid water)}$$

$$c_p = 1004 \text{ J kg}^{-1} \text{ K}^{-1} \text{ (specific heat at constant pressure for dry air)}$$

$$c_v = 717 \text{ J kg}^{-1} \text{ K}^{-1} \text{ (specific heat at constant volume for dry air)}$$

$$R_d = c_p - c_v = 287 \text{ J kg}^{-1} \text{ K}^{-1} \text{ (gas constant for dry air)}$$

$$R^* = 8.31 \text{ J mol}^{-1} \text{ K}^{-1} \text{ (universal gas constant)}$$

$$m_d = 28.97 \text{ g mol}^{-1} \text{ (mean molecular weight of dry air)}$$

$$m_v = 18.02 \text{ g mol}^{-1} \text{ (molecular weight of water vapor)}$$

$$L_e = 2.5 \times 10^6 \text{ J kg}^{-1} \text{ (latent heat of evaporation)}$$