



~100 m

**Turbulent Mixing**

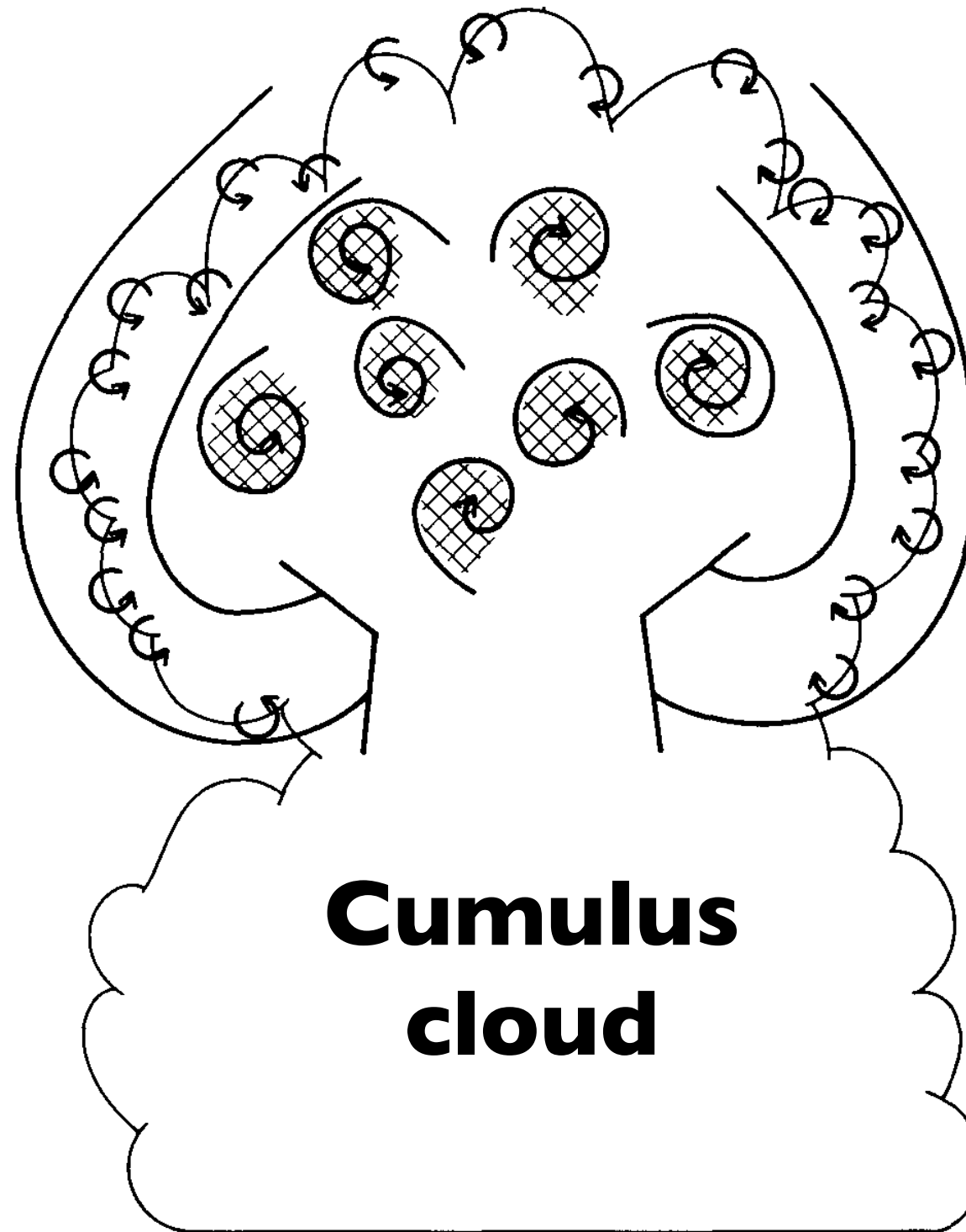
# Kelvin-Helmholtz Instability: $Re=900$ and $1400$



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# Entrainment and Mixing

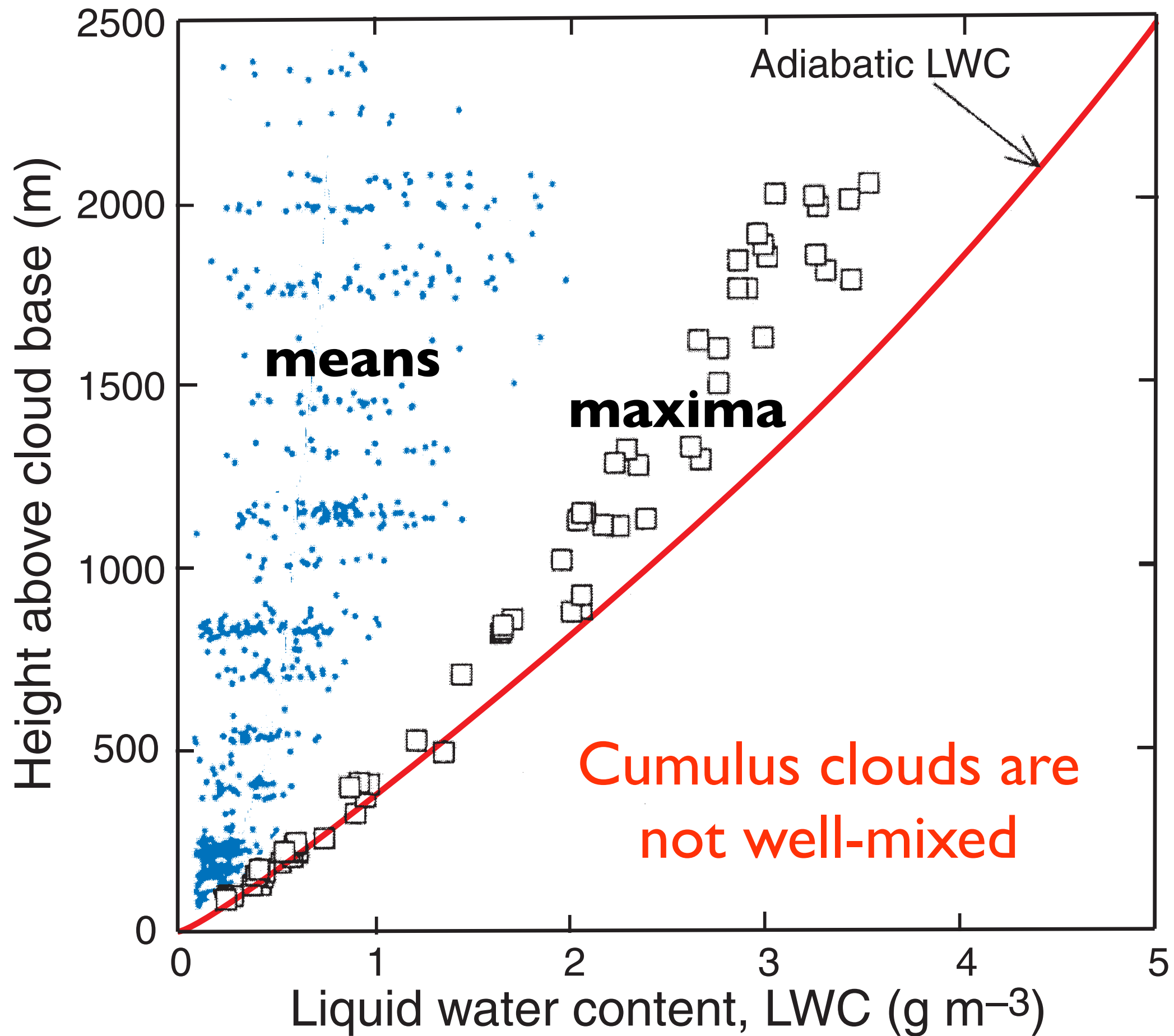


# Mixing Time Scale

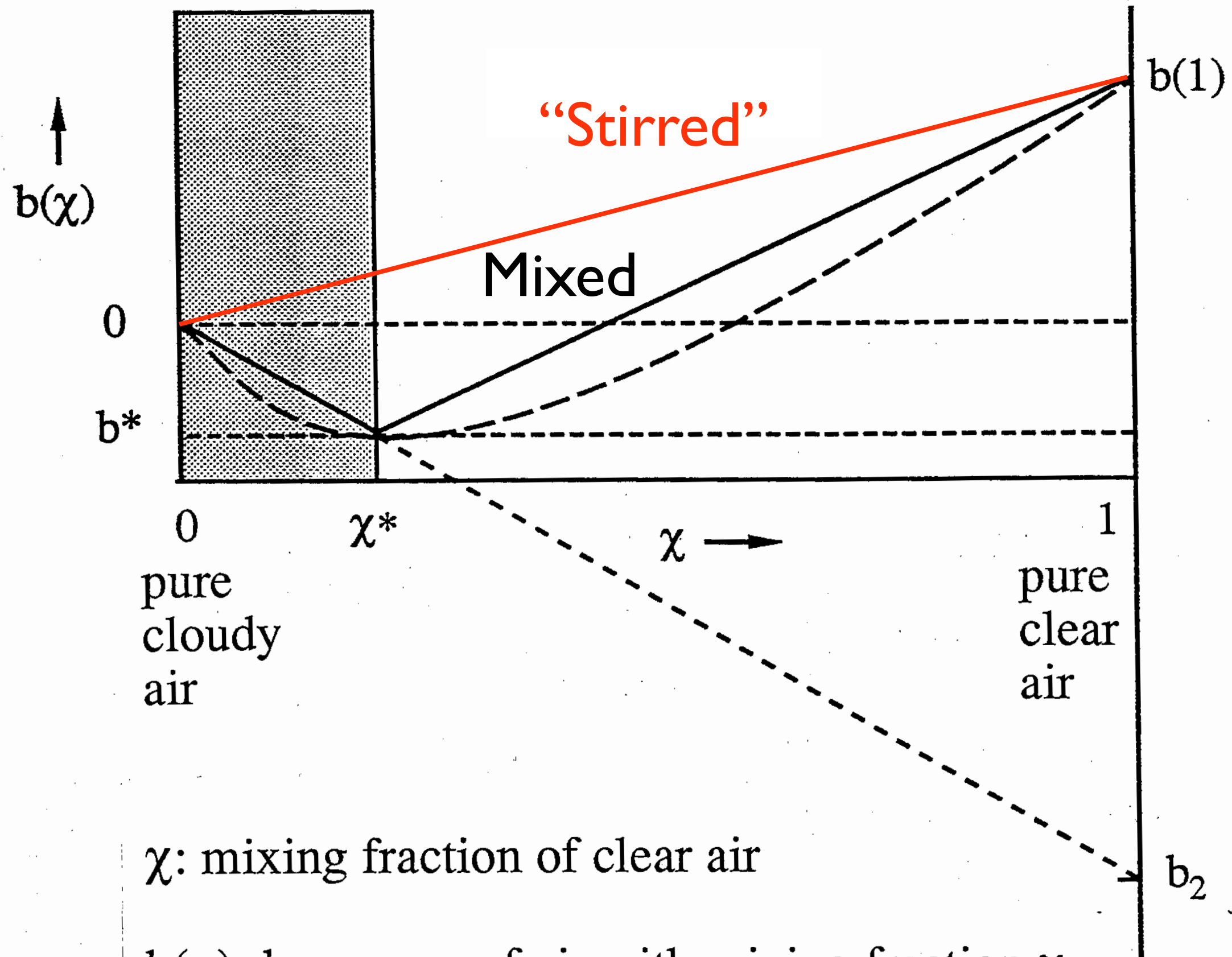
$$\tau = \left( \frac{d^2}{\epsilon} \right)^{1/3},$$

$d$  is entrained blob size,  $\epsilon$  is dissipation rate of turbulence kinetic energy.

For a **cumulus cloud**,  $U \sim 2$  m/s,  $L \sim 1000$  m, so  $\epsilon \sim U^3/L = 10^{-2}$  m<sup>2</sup>/s<sup>3</sup>. For  $d = 100$  m,  $\tau \sim 100$  s.



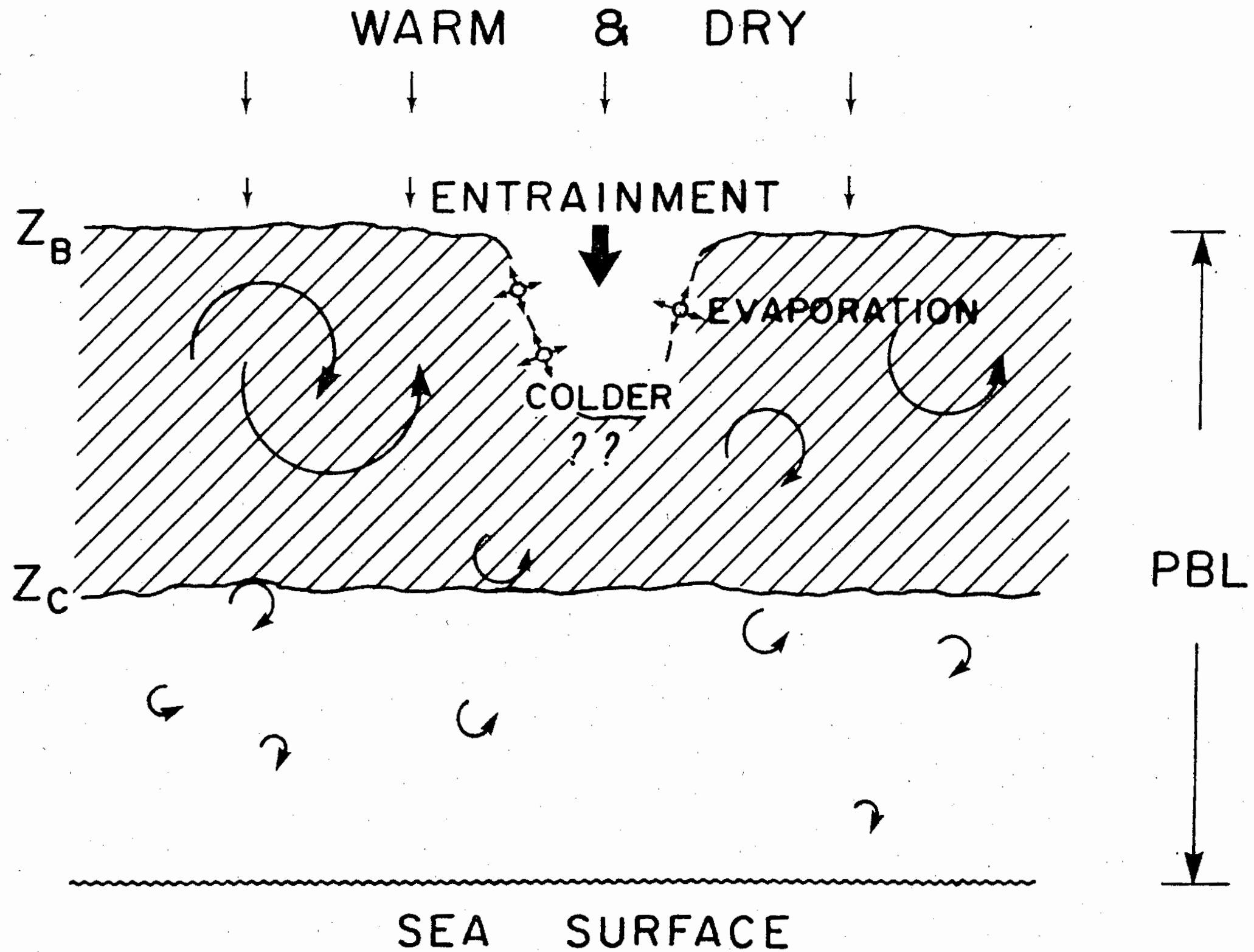
# Buoyancy vs Mixture Fraction



$\chi$ : mixing fraction of clear air

$b(\chi)$ : buoyancy of air with mixing fraction  $\chi$

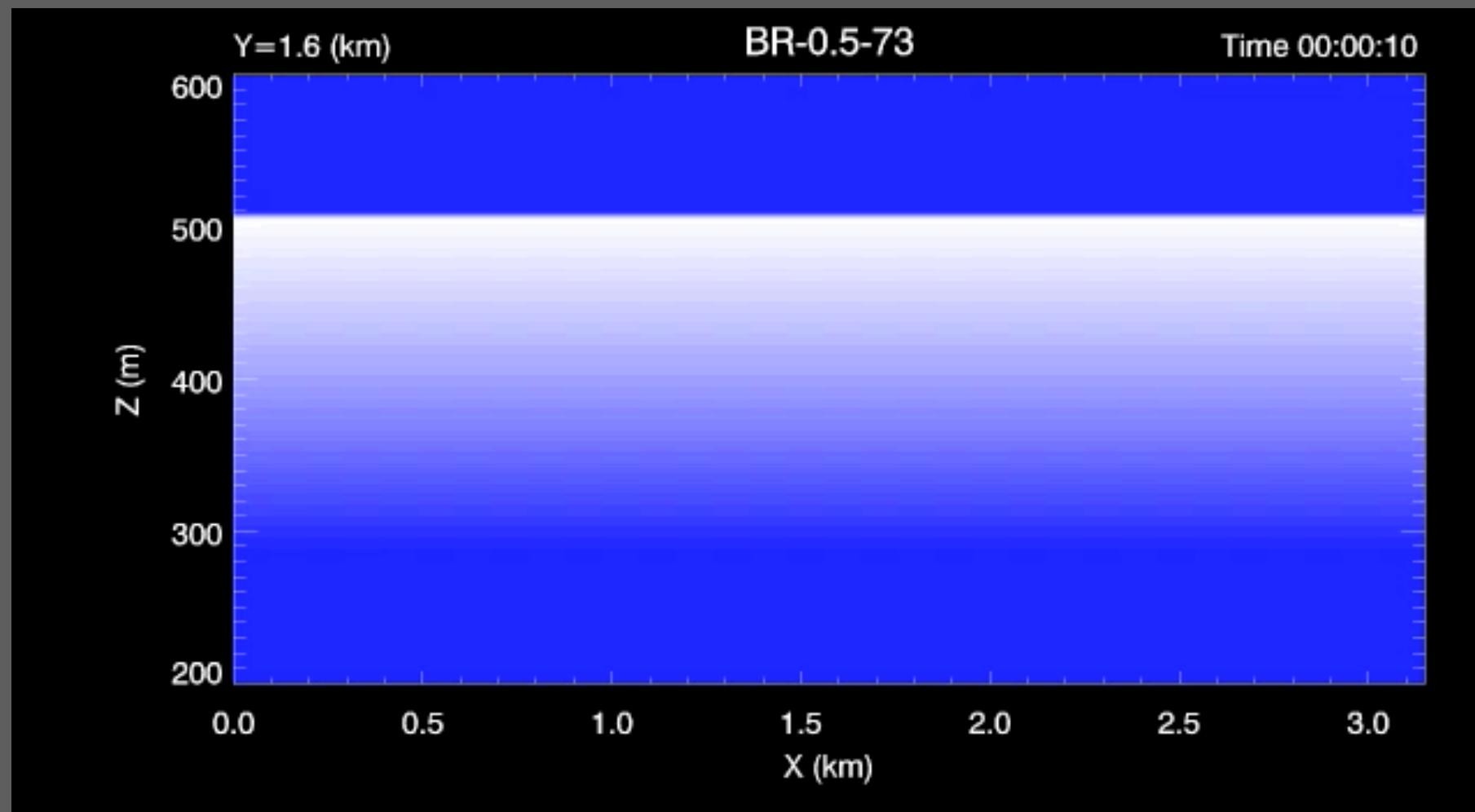
# Cloud-top Entrainment Instability (CEI)





# LES with a 5-m isotropic grid (Yamaguchi and Randall 2008)

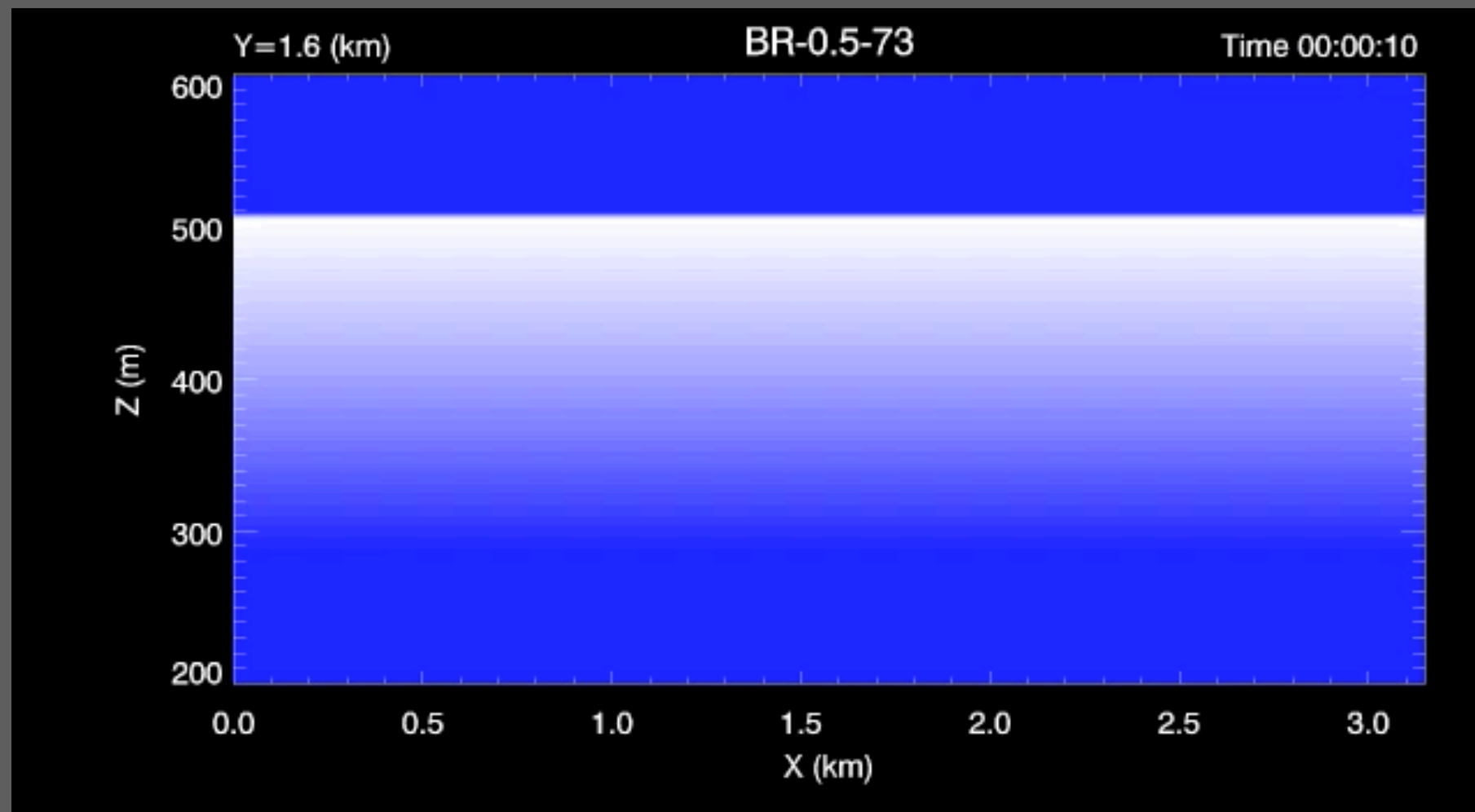
Yamaguchi, T., and D. A. Randall, 2008: Large-eddy simulation of evaporatively driven entrainment in cloud-topped mixed layers. *J. Atmos. Sci.*, 65, 1481–1504.



- Newly entrained thermals tend to follow the dry paths of earlier thermals.
- The dry paths become wider.

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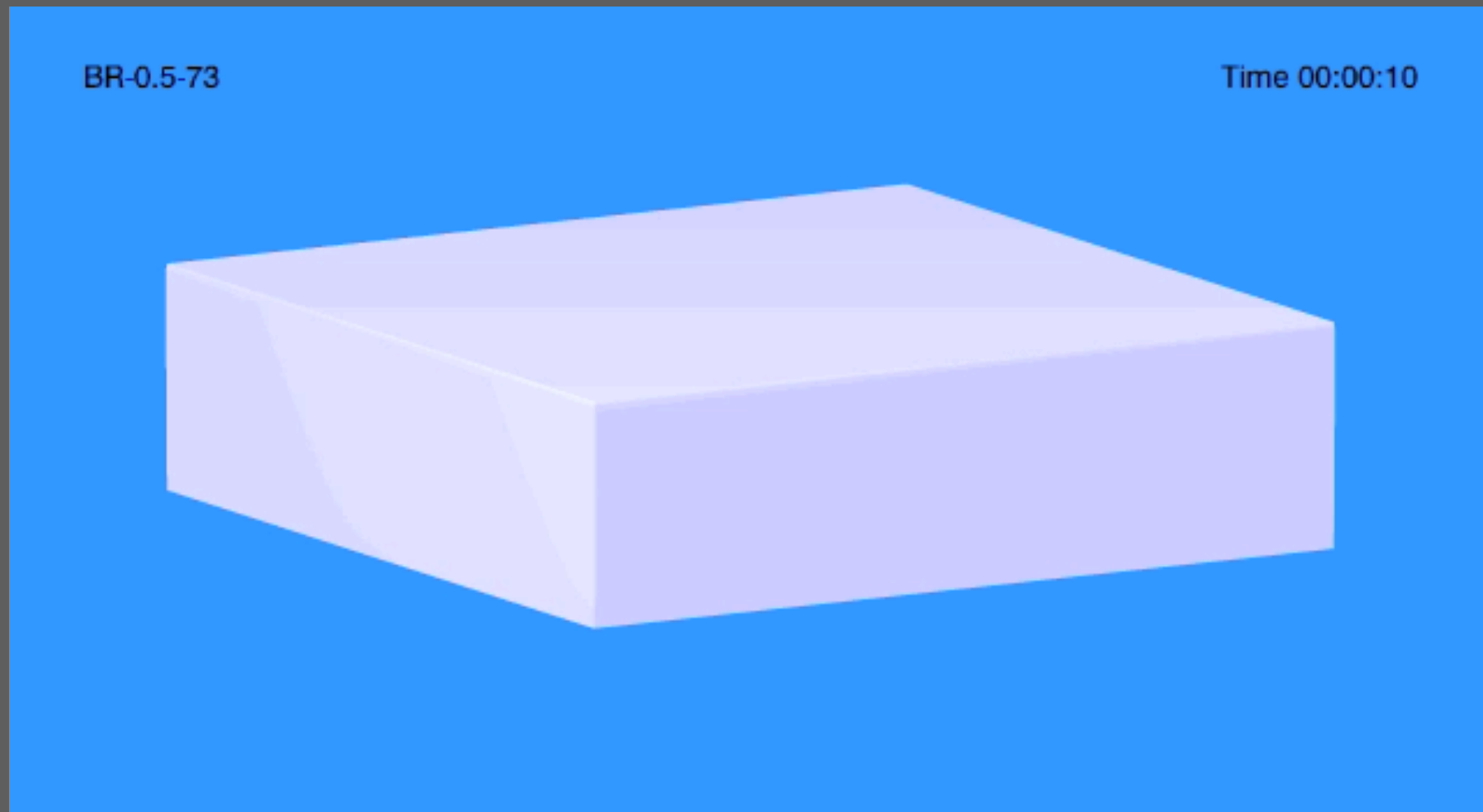
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